

# An Algorithm for Creating Puzzles

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[oddsandevenings.com](http://oddsandevenings.com)

Snow White is trying to get the seven dwarfs to sit down around their circular table, but it turns out they are a fussy lot and some of them are point blank refusing to sit next to others.

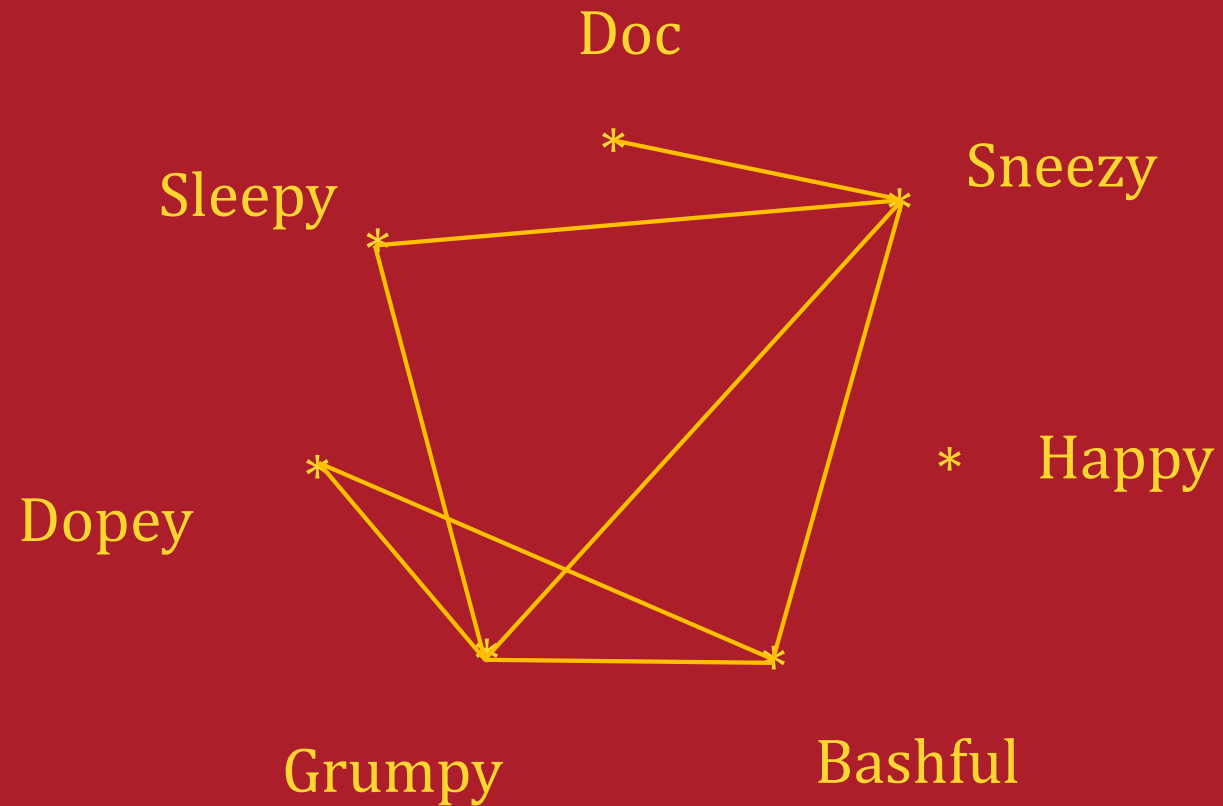
Doc is worried he may get an infection from Sneezy, while Dopey, Sneezy and Bashful are all a bit frightened of Grumpy while he's in one of his tempers. Bashful had an awful falling out in the mine with Dopey and Sneezy and finally Sleepy doesn't want to be woken up by the loud noises from Sneezy or Grumpy.

Who's sat next to Happy?

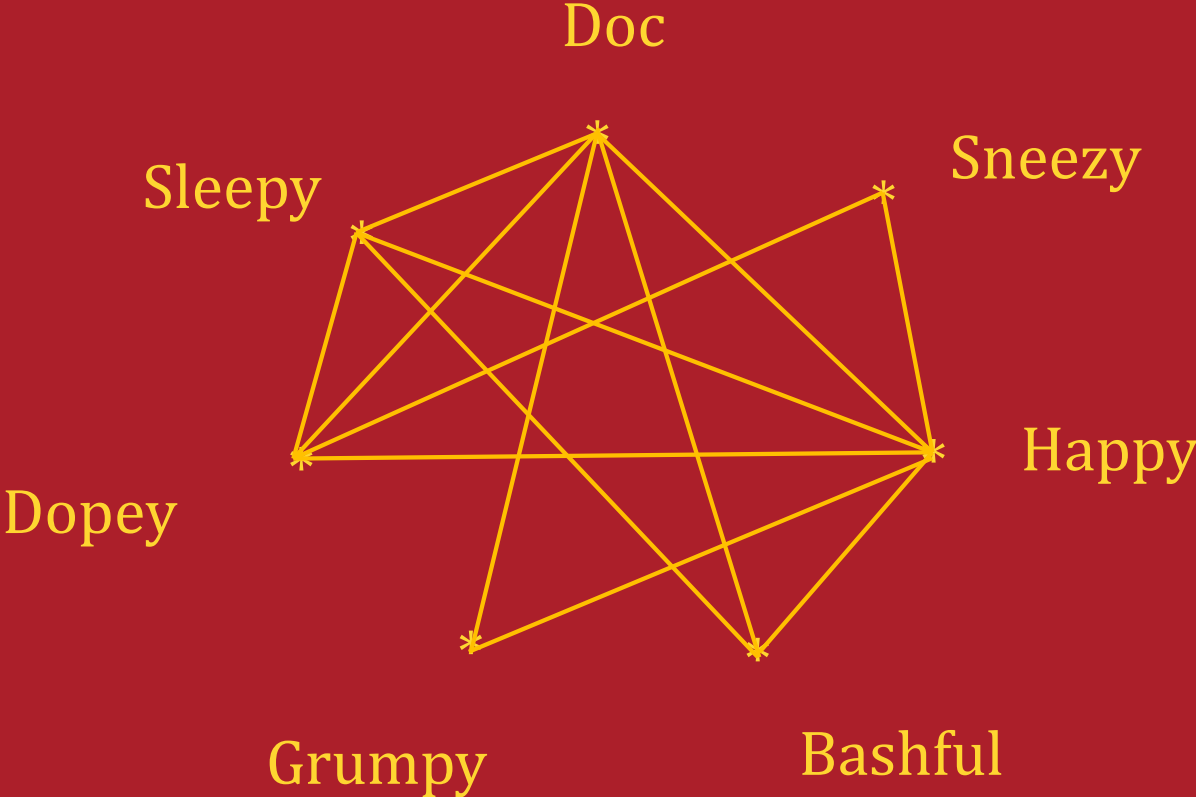
# Making it easier



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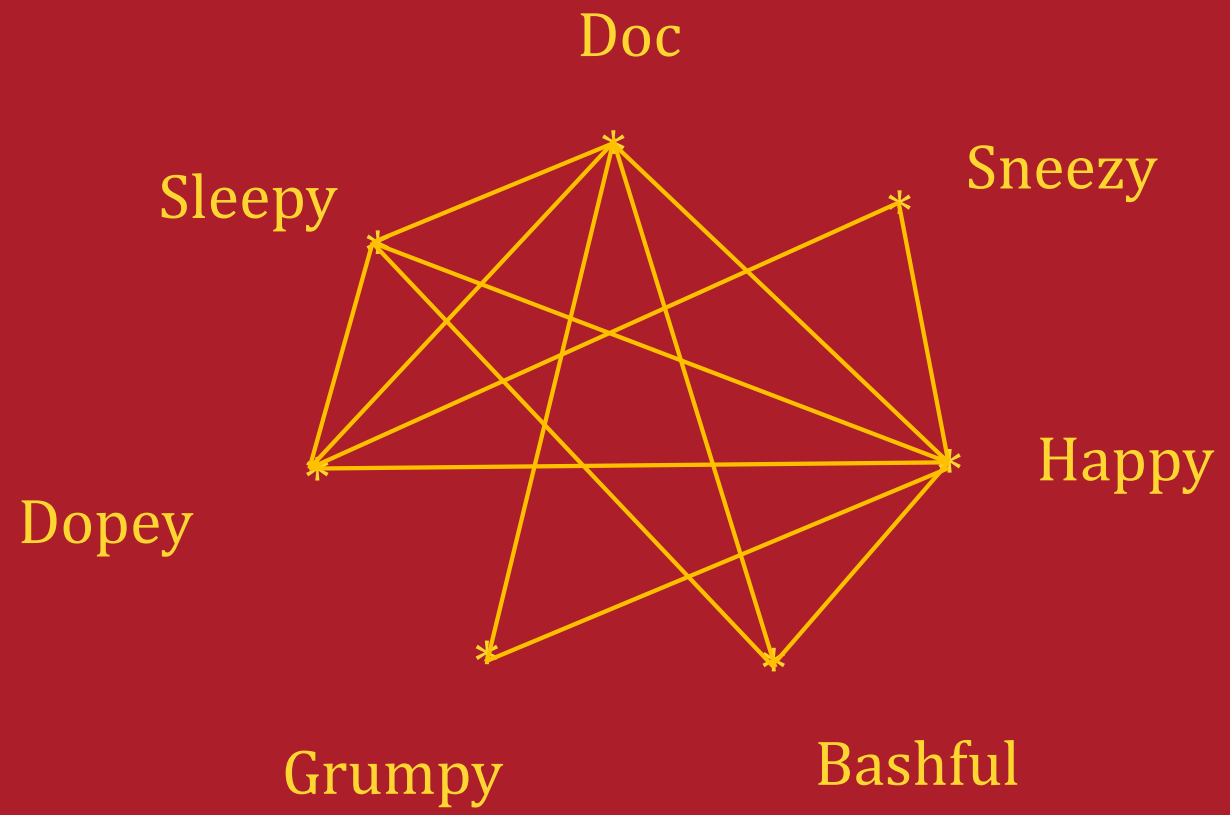


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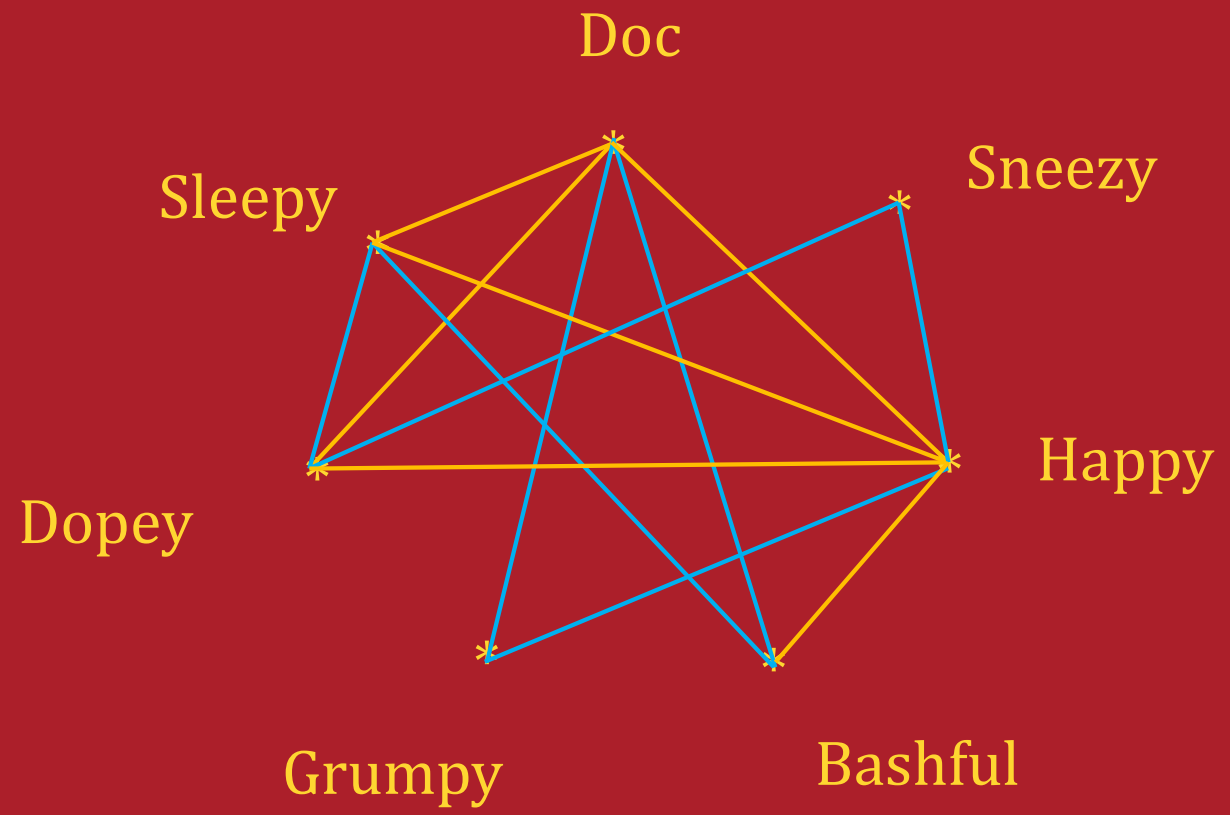
# Making it easier

# Find a Hamiltonian Cycle



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# What do we want from the algorithm?

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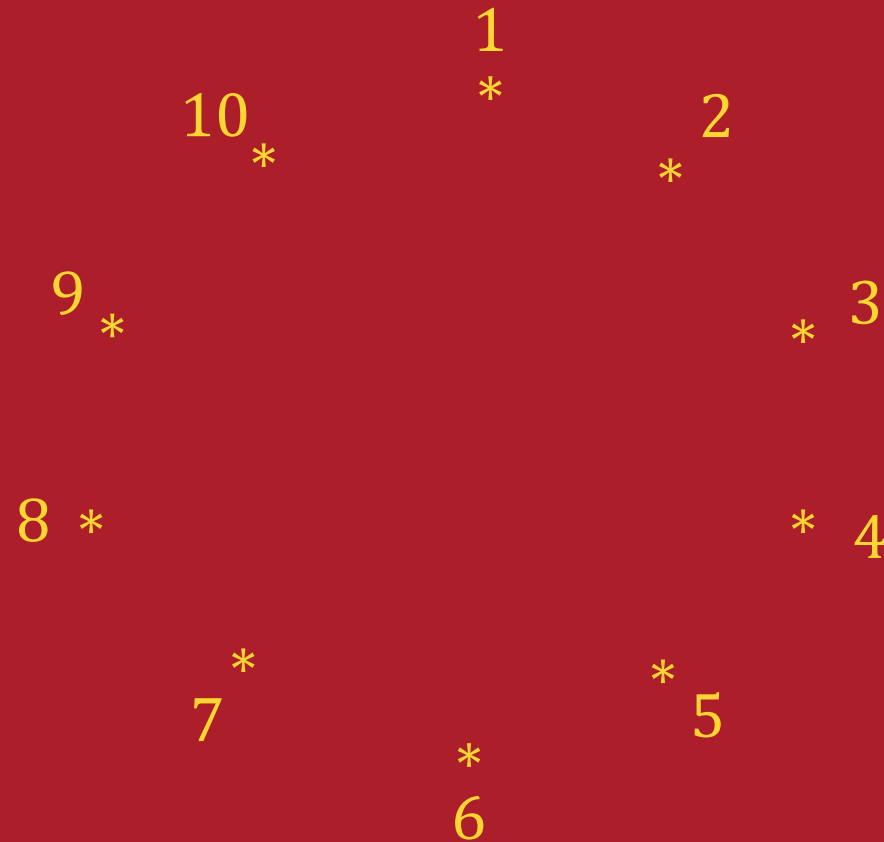
1. Unique Hamiltonian Cycle

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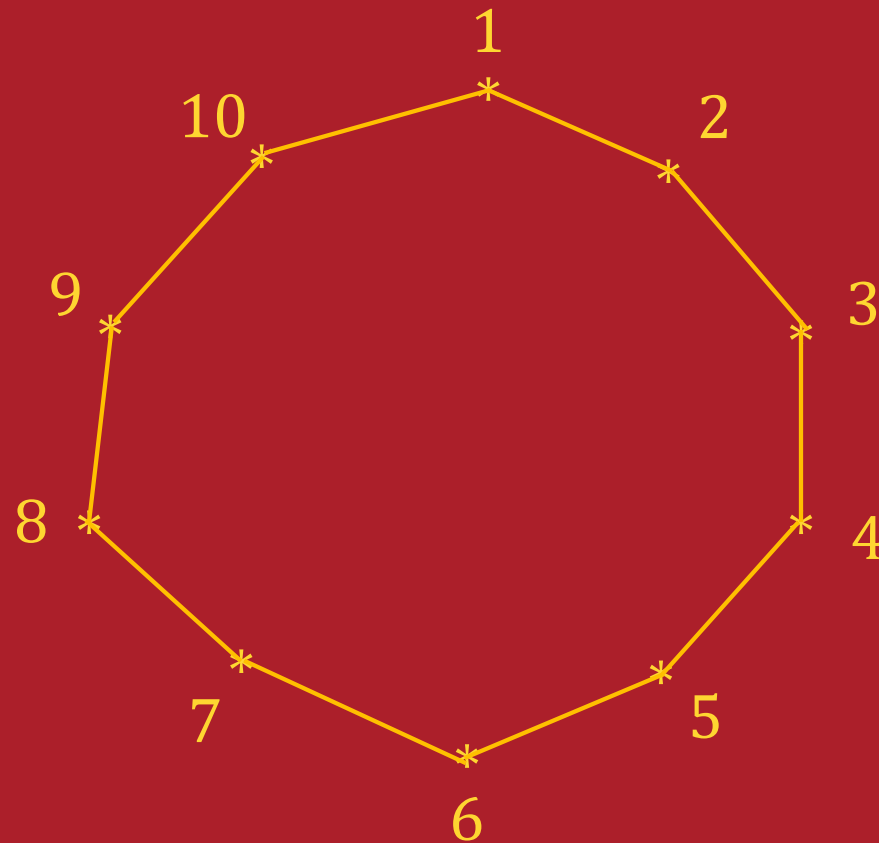
2. A Relatively Dense Graph

# The Algorithm



Draw and label n points

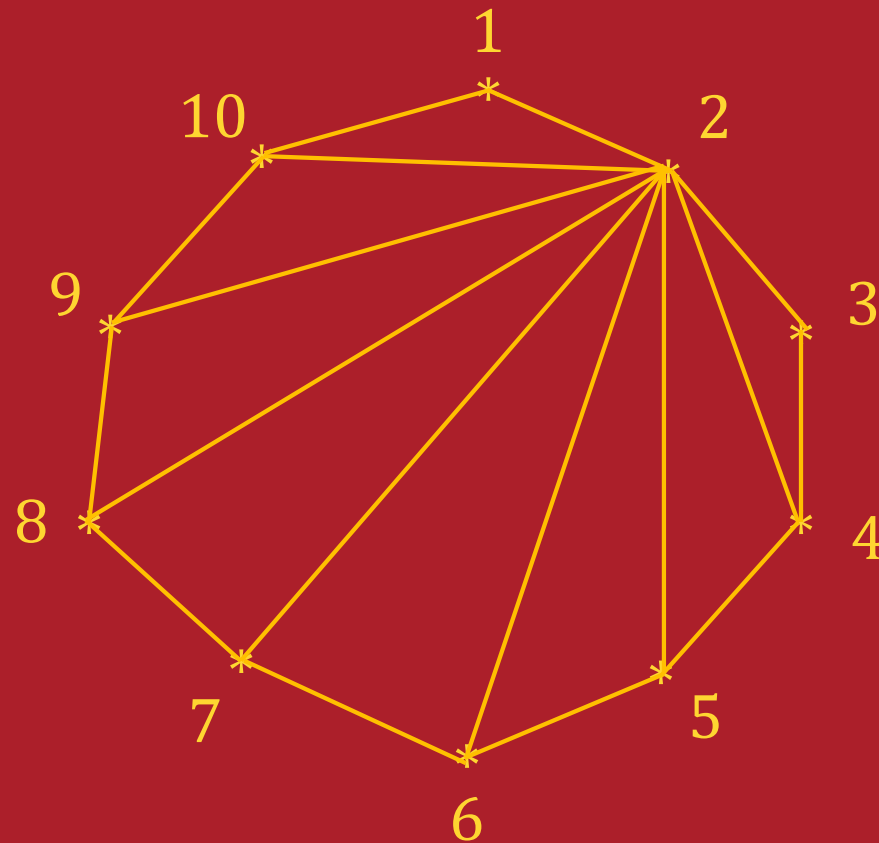
# The Algorithm



Connect the nodes  
around the edge

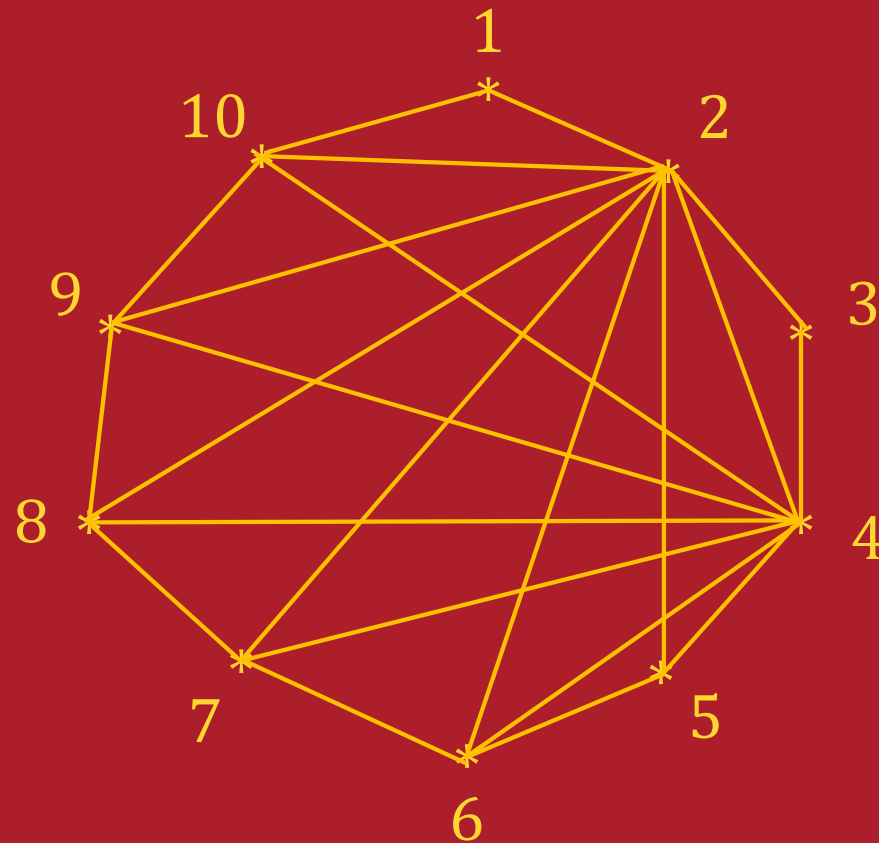
This will be our  
solution

# The Algorithm



Connect every even node to every node above it

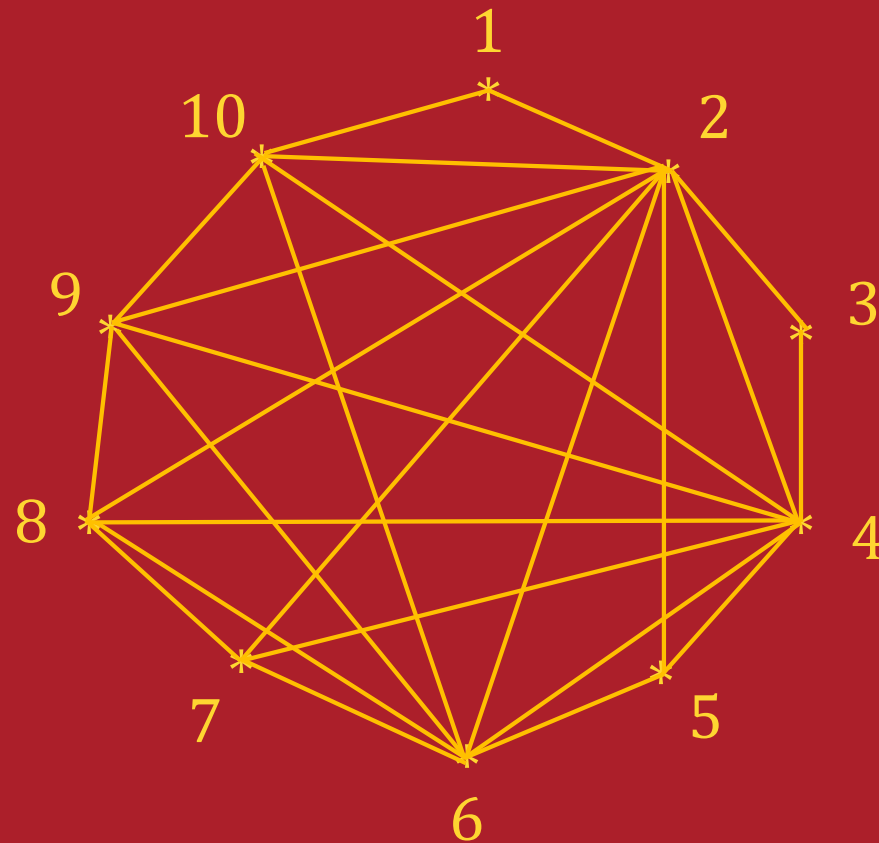
# The Algorithm



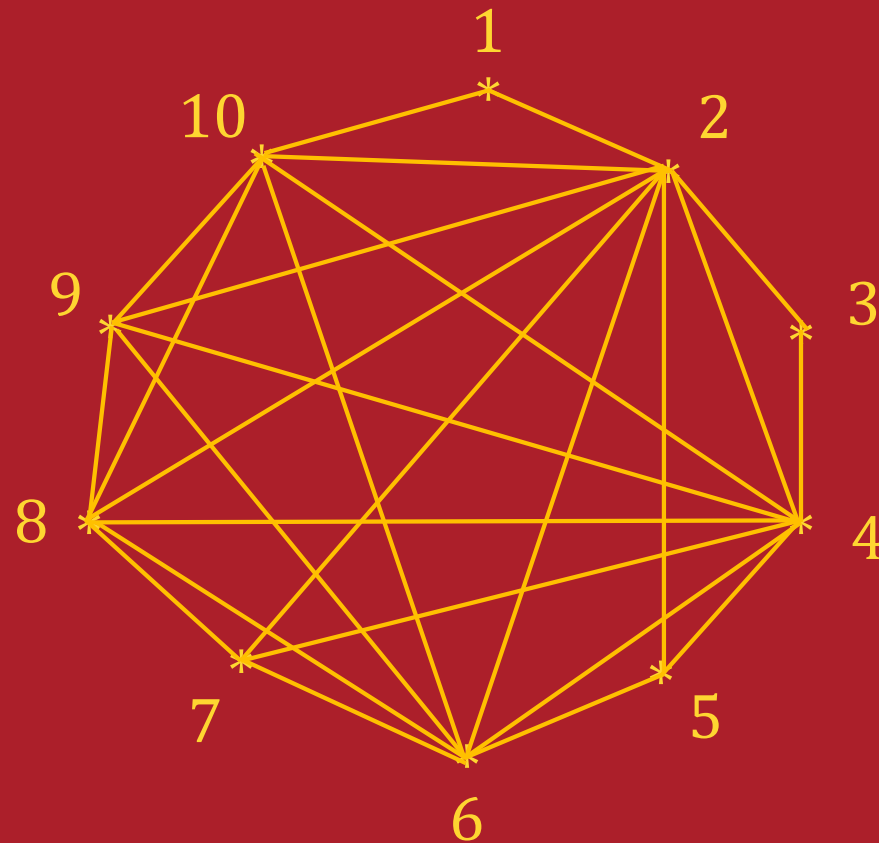
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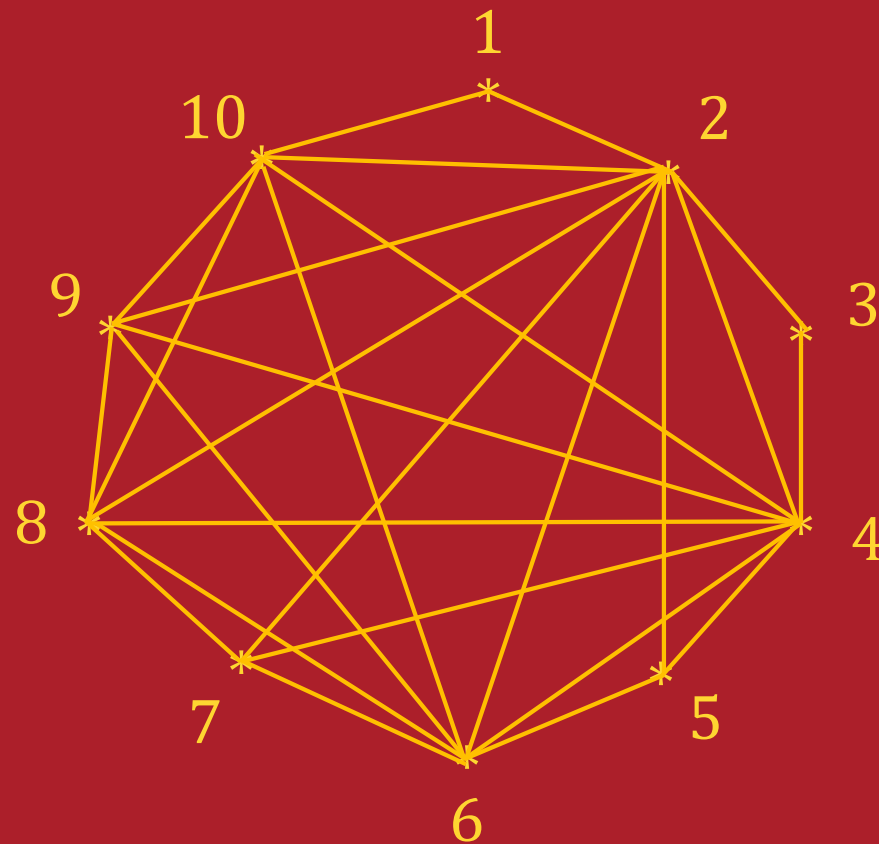
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# The Algorithm

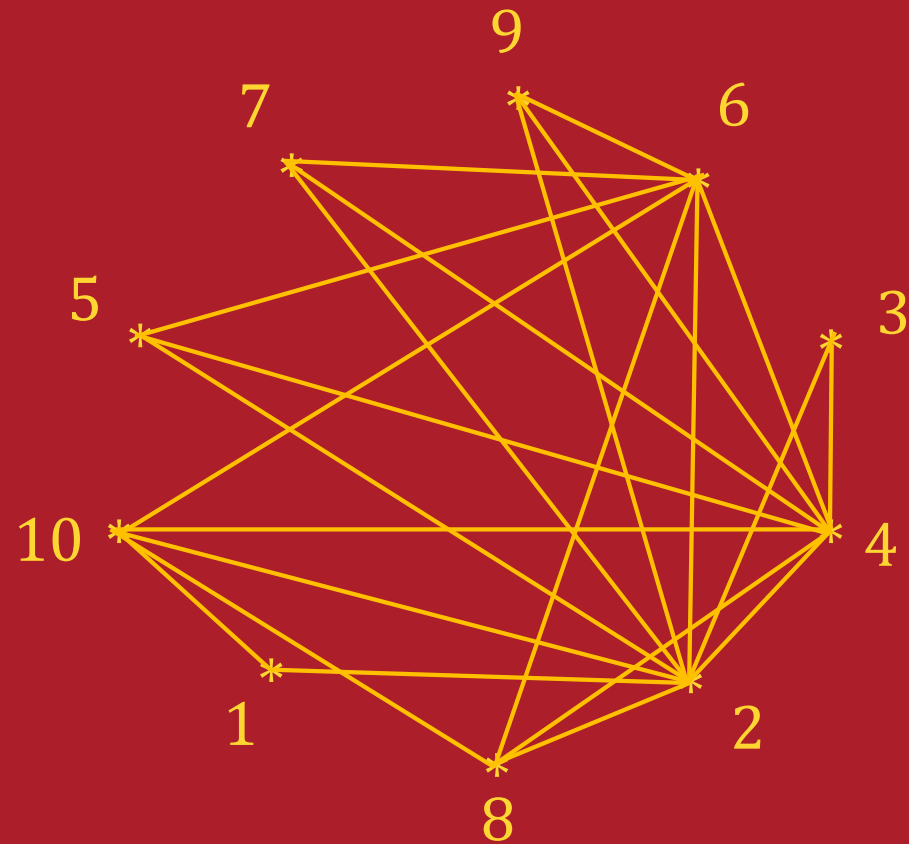


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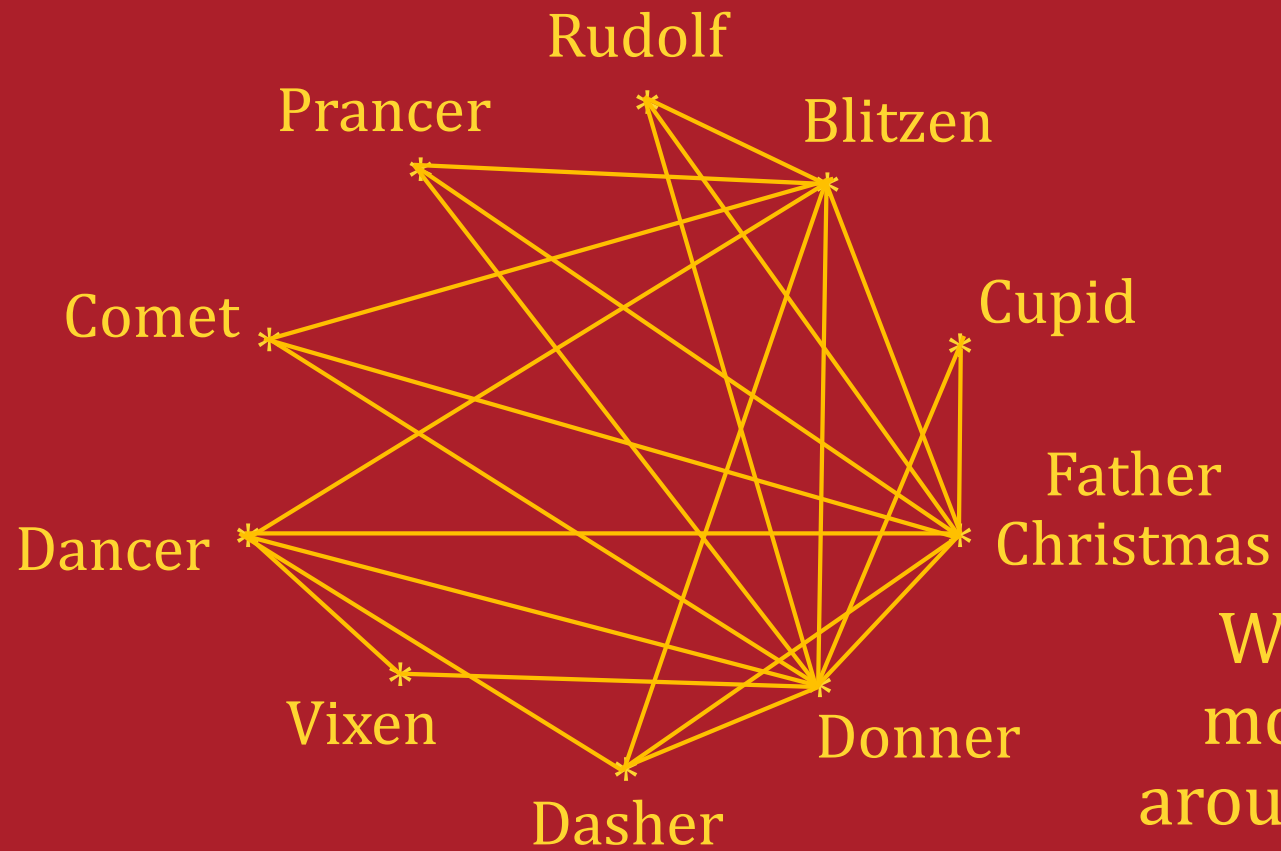


This has a unique Hamiltonian Cycle (around the edge)

We can hide it by moving the points around and relabeling

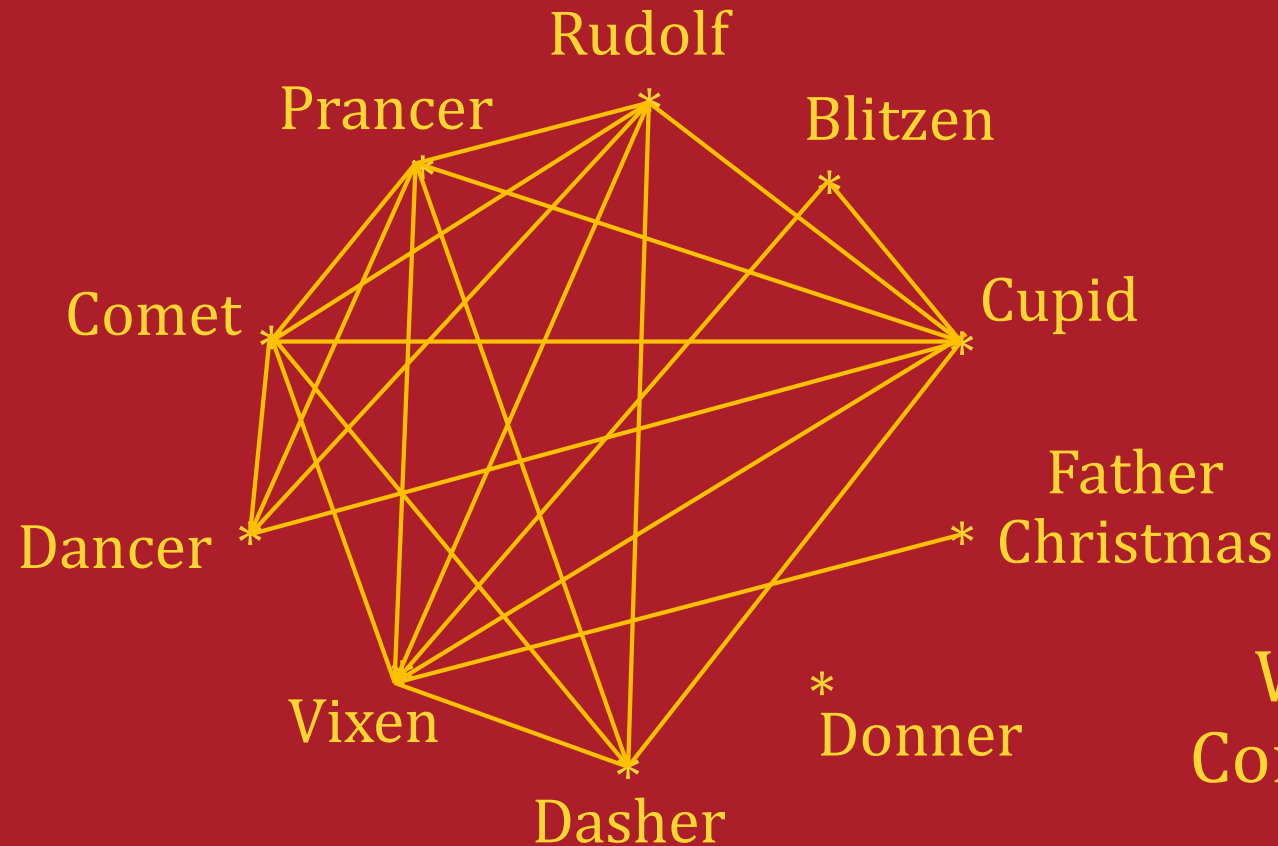


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# Optional (to make a word puzzle)



We can use the  
Compliment Graph

This process can make  
puzzles to an arbitrary  
level of difficulty

I cohost a Maths and Puzzles podcast:

[www.oddsandevenings.com](http://www.oddsandevenings.com)

(or wherever you normally get your podcasts)