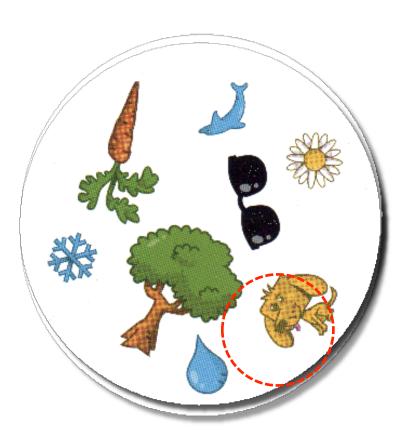
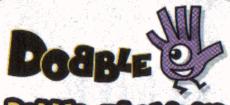




How do they do that?







Dobble, what is it?

Dobble consists of 55 cards, with 8 symbols per card from the 50 available. There is **only one identical symbol** in common between each card, it is up to you to find out which one.

Before playing...

If you've never played or if you're playing with people who've never played before, draw two random cards and place them face-up on the table between all the players. Look

for the identical symbol between the two cards

(same shape, same color, only the size can be different). The first player to find the right symbol names it out loud and draws two new cards which are then placed face-up on the table. Repeat this until each player understands

that there's always only one identical symbol between two cards.

How do they do that?

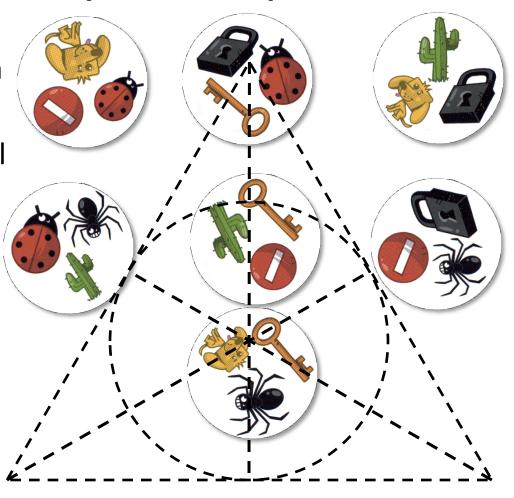
Simpler case: 3 symbols per card

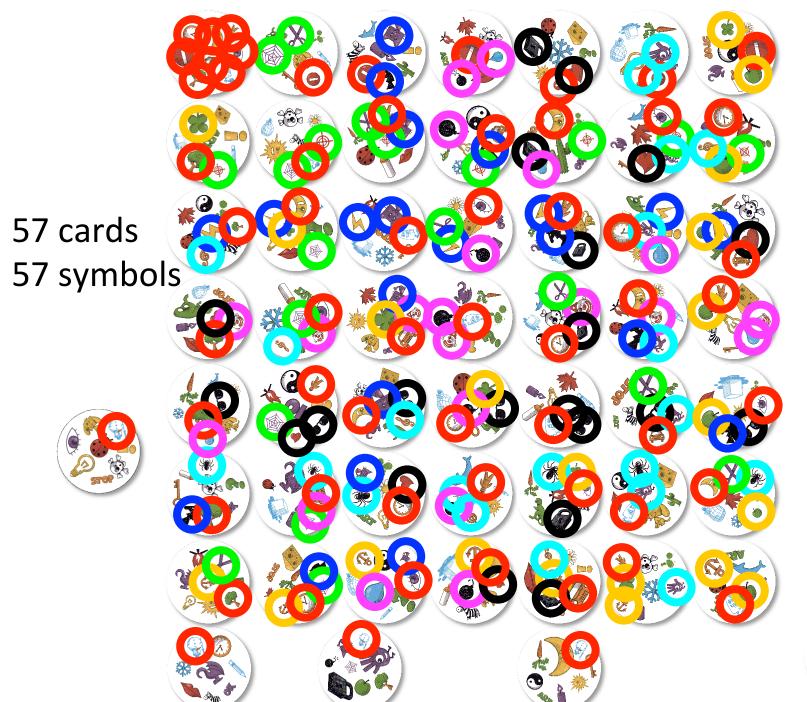
1 symbol for every line.

Every pair of cards lie on a unique line...

...so have a unique symbol in common.

- Fano plane
- Finite projective plane of order N=2.
 - $-N^2+N+1$ points, lines
 - N+1 symbols/card
- Dobble: N=7
 - 8 symbols/card
 - 57 points (cards)
 - 57 lines (symbols)









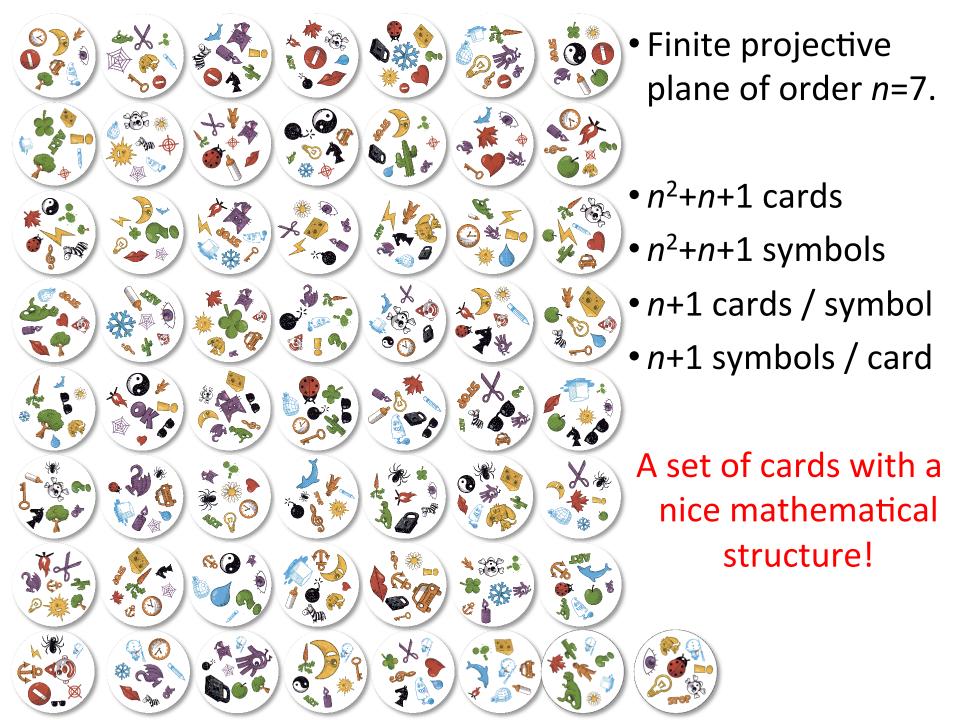






- Assign a symbol to cards on a straight line.
- Each pair of cards define a unique line...
- ...so have a unique symbol in common!
- 7 parallel lines per direction.
- 8 directions...
- Can assign extra cards for intersection of parallel lines.
- These also need a symbol in common.

49 cards
58 symbols





...almost.

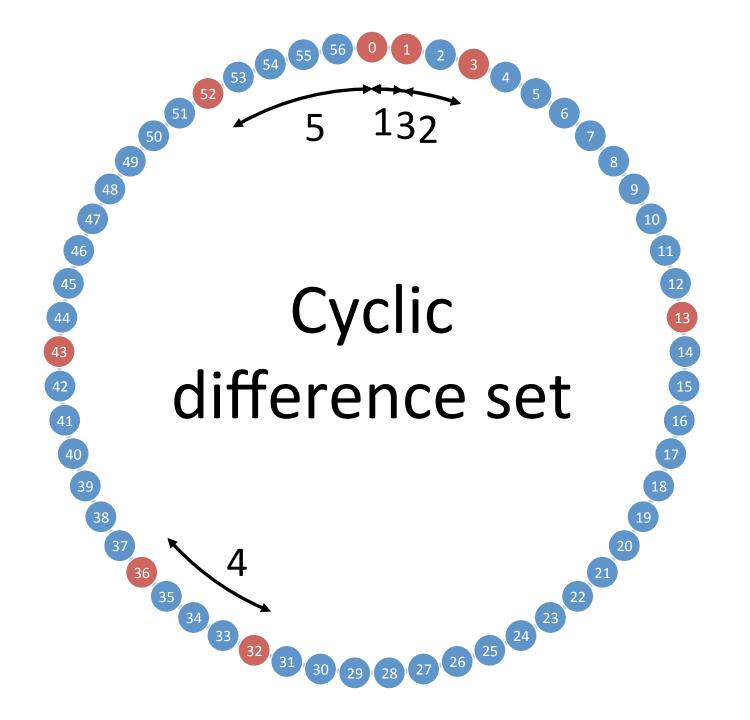


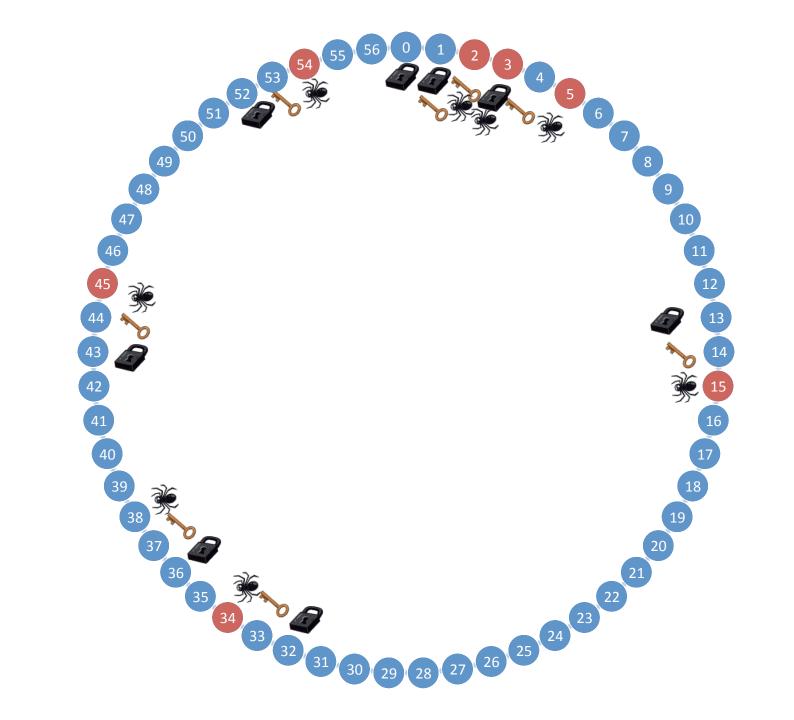
Another representation of the structure

| 0 | | 9 | | 18 | | 27 | 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 36 | P | 45 | | 54 | *** |
|---|---|----|--|----|------|----|--|----|-------|----|----------|----|-----|
| 1 | | 10 | The state of the s | 19 | | 28 | | 37 | | 46 | | 55 | |
| 2 | | 11 | ************************************** | 20 | | 29 | ART SU | 38 | | 47 | X A | 56 | |
| 3 | | 12 | 200 M | 21 | * 23 | 30 | *** | 39 | - 200 | 48 | | | |
| 4 | | 13 | | 22 | * VO | 31 | 100 mm | 40 | | 49 | | | |
| 5 | | 14 | * X ** | 23 | | 32 | | 41 | | 50 | * 200° 8 | | |
| 6 | | 15 | | 24 | *** | 33 | | 42 | | 51 | | | |
| 7 | 1 | 16 | *** | 25 | | 34 | S * | 43 | | 52 | | | |
| 8 | | 17 | 10 | 26 | | 35 | | 44 | *** | 53 | | | |

Matching symbols occur at relative positions (mod 57) 0, 1, 3, 13, 32, 36, 43, 52

What is special about these numbers that makes this ordering possible?





| 0 | | 9 | | 18 | | 27 | 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 | 36 | P | 45 | | 54 | *** |
|---|---|----|--|----|------|----|--|----|-------|----|----------|----|-----|
| 1 | | 10 | The state of the s | 19 | | 28 | | 37 | | 46 | | 55 | |
| 2 | | 11 | ************************************** | 20 | | 29 | ART SU | 38 | | 47 | X A | 56 | |
| 3 | | 12 | 200 M | 21 | * 23 | 30 | *** | 39 | - 200 | 48 | | | |
| 4 | | 13 | | 22 | * VO | 31 | 100 mm | 40 | | 49 | | | |
| 5 | | 14 | * X ** | 23 | | 32 | | 41 | | 50 | * 200° 8 | | |
| 6 | | 15 | | 24 | *** | 33 | | 42 | | 51 | | | |
| 7 | 1 | 16 | *** | 25 | | 34 | S * | 43 | | 52 | | | |
| 8 | | 17 | 10 | 26 | | 35 | | 44 | *** | 53 | | | |